

Math 172 Quiz 7

Sections: 10.5-6

9 November 2018

Name: _____

Point values in boxes.

1. [2] Please circle True or False, as appropriate.

(a) T / F : In the Ratio Test, if $\lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right| \geq 1$, the series $\sum a_n$ diverges.

(b) T / F : $\sum a_n x^n$, if $\lim_{n \rightarrow \infty} \left| \frac{a_{n+1} x^{n+1}}{a_n x^n} \right| = 5|x|$, the radius of convergence R is 1/5.

(c) T / F : $\sum a_n (x - c)^n$, if $\lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right| = \infty$, the radius of convergence is 0.

(d) T / F : $\sum a_n (x - 1)^n$ converges when $x = 0$, it must converge when $x = 2$.

2. [3] For each of the following series, circle if they converge or diverge and circle the test you used.
(No justification required.)

$$\sum_{n=1}^{\infty} \left(\frac{-2}{n} \right)^n$$

converges

diverges

Divergence test

Integral Test

Root Test

$$\sum_{n=1}^{\infty} (-1)^n \cos \frac{1}{n}$$

converges

diverges

Divergence test

Alternating Series Test

Ratio Test

$$\sum_{n=1}^{\infty} \frac{n}{2n^2 + 1}$$

converges

diverges

Ratio Test

Limit Comparison Test

Divergence Test

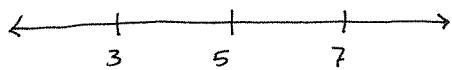
CONTINUED ON REVERSE.

3. [5] For the power series below, find and clearly state the radius and interval of convergence.
Justification required: identify the tests you use, verify assumptions, and write conclusions.

$$\sum_{n=1}^{\infty} \frac{(-1)^n (x-5)^n}{n 2^n}$$

$$\sqrt[n]{\left| \frac{(-1)^n (x-5)^n}{n 2^n} \right|} \xrightarrow{n \rightarrow \infty} \frac{|x-5|}{2} < 1 \quad \text{when } |x-5| < 2$$

Radius



$$x = 3 : \sum_{n=1}^{\infty} \frac{(-1)^n (-2)^n}{n 2^n} = \sum_{n=1}^{\infty} \frac{1}{n} \quad \text{which is the Divergent Harmonic Series.}$$

$$x = 7 : \sum_{n=1}^{\infty} \frac{(-1)^n 2^n}{n 2^n} = \sum_{n=1}^{\infty} \frac{(-1)^n}{n} \quad \text{which converges by the}\\ \text{Alternating Series Test since}$$

$$\frac{1}{n} > 0, \quad \frac{1}{n} > \frac{1}{n+1}, \quad \text{and} \quad \frac{1}{n} \xrightarrow{n \rightarrow \infty} 0.$$

So the interval of convergence is $I = (3, 7]$.