

1. 2 Please indicate True or False. Assume the vectors \mathbf{u} and \mathbf{v} are non-zero.

(a) T / F $\mathbf{u} \cdot \mathbf{u} = 0$

(b) T / F $\mathbf{u} \times \mathbf{u} = \mathbf{0}$

(c) T / F $\|\mathbf{u}_{\parallel\mathbf{v}} + \mathbf{u}_{\perp\mathbf{v}}\| = \|\mathbf{u}\|$

(d) T / F $\mathbf{k} \times \mathbf{j} = -\mathbf{i}$

2. 4 Find the decomposition of $\mathbf{u} = \langle 3, -5, -7 \rangle$ along $\mathbf{v} = \langle 1, 2, 3 \rangle$, i.e. find $\mathbf{u}_{\parallel\mathbf{v}}$ and $\mathbf{u}_{\perp\mathbf{v}}$.

$$\vec{u}_{\parallel\vec{v}} = \frac{\vec{u} \cdot \vec{v}}{\vec{v} \cdot \vec{v}} \vec{v} = \frac{3-10-21}{1+4+9} \vec{v} = \frac{-28}{14} \vec{v} = -2 \vec{v} = \langle -2, -4, -6 \rangle$$

$$\vec{u}_{\perp\vec{v}} = \vec{u} - \vec{u}_{\parallel\vec{v}} = \langle 3, -5, -7 \rangle - \langle -2, -4, -6 \rangle = \langle 5, -1, -1 \rangle$$

3. 4 Find a unit vector orthogonal to both $\mathbf{u} = \langle 1, 2, 3 \rangle$ and $\mathbf{v} = \langle 0, 1, 2 \rangle$.

$$\begin{aligned} \vec{u} \times \vec{v} &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 3 \\ 0 & 1 & 2 \end{vmatrix} = (4-3)\hat{i} - (2-0)\hat{j} + (1-0)\hat{k} \\ &= \langle 1, -2, 1 \rangle \end{aligned}$$

$$\vec{e}_{\vec{u} \times \vec{v}} = \frac{1}{\sqrt{6}} \langle 1, -2, 1 \rangle$$