

## Exam 2

- **Variation of Parameters**

If  $y_1$  and  $y_2$  are linearly independent solutions to  $y'' + p(t)y' + q(t)y = 0$ , then a particular solution to  $y'' + p(t)y' + q(t)y = g(t)$  is given by

$$y_p(t) = y_1(t) \int \frac{-g(t)y_2(t)}{W[y_1, y_2](t)} dt + y_2(t) \int \frac{g(t)y_1(t)}{W[y_1, y_2](t)} dt.$$

- **Reduction of Order**

If  $y_1(t)$  is a solution, not identically zero, to  $y'' + p(t)y' + q(t)y = 0$  on  $I$ , then

$$y_2(t) = y_1(t) \int \frac{e^{-\int p(t) dt}}{(y_1(t))^2} dt$$

is a second, linearly independent solution.

- **A Trigonometric Identity**

$A \cos \theta + B \sin \theta = C \cos(\theta - \phi)$  where  $C = \sqrt{A^2 + B^2}$  and  $\phi = \begin{cases} \arctan(B/A), & A > 0 \\ \arctan(B/A) + \pi, & A < 0, B > 0 \\ \arctan(B/A) - \pi, & A < 0, B < 0 \end{cases}$