

Math 274 Quiz 2

Sections: 2.2-2.4

7 September 2018

Name: _____ Point values in

1. [5] Find an implicit general solution of

$$x^2 y' = y \ln y - y'. \quad \leftarrow \text{See # 9 in § 2.2}$$

$$(x^2 + 1) \frac{dy}{dx} = y \ln y$$

$$\int \frac{dy}{y \ln y} = \int \frac{dx}{x^2 + 1}$$

$$\ln(\ln y) = \arctan x + C$$

Note: solutions of the form $y \equiv 1$ got lost

2. [5] Find a general solution of

$$xy' + 2y = e^{-2x}.$$

$$y' - \left(-\frac{2}{x}\right)y = \frac{e^{-2x}}{x}$$

$$u(x) = e^{-\int -\frac{2}{x} dx} = e^{2 \ln|x|} = x^2$$

$$\text{so } y = \frac{1}{x^2} \left(-\frac{x e^{-2x}}{2} - \frac{e^{-2x}}{4} + C \right)$$

$$x^2 y' + 2x y = x e^{-2x}$$

$$(x^2 y)' = x e^{-2x}$$

$$x^2 y = \int x e^{-2x} dx$$

$$= -\frac{x e^{-2x}}{2} - \frac{e^{-2x}}{4} + C$$

see quiz 1