

Find the general solution for the following.

1. 2 $y'' + 5y' + 4y = 0$

$$r^2 + 5r + 4 = 0$$

$$(r+4)(r+1) = 0$$

$$r = -1, -4$$

$$y = C_1 e^{-t} + C_2 e^{-4t}$$

2. 2 $y'' + 4y' + 4y = 0$

$$(r+2)^2 = 0$$

$$y = C_1 e^{-2t} + C_2 t e^{-2t}$$

3. 2 $y'' + 3y' + 4y = 0$

$$r^2 + 3r + 4 = 0$$

$$r = \frac{-3 \pm \sqrt{9-16}}{2} = \frac{-3 \pm i\sqrt{7}}{2}$$

$$y = C_1 e^{-3t/2} \cos\left(\frac{\sqrt{7}}{2}t\right) + C_2 e^{-3t/2} \sin\left(\frac{\sqrt{7}}{2}t\right)$$

4. 2 $y'' = 0$

$$r^2 = 0$$

$$r = 0$$

$$y = C_1 + C_2 t$$

5. 2 $z''' + 2z'' - 4z' - 8z = 0$

$$r^3 + 2r^2 - 4r - 8 = 0$$

$$r^2(r+2) - 4(r+2) = 0$$

$$(r-2)(r+2)^2 = 0$$

$$y = C_1 e^{2t} + C_2 e^{-2t} + C_3 t e^{-2t}$$