

**Math 274 Homework**

Sections: 7.2,7.3

Due: 24 May 2018

Name: \_\_\_\_\_  
Point Values in 

boxes
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1. 

2
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 For what values of  $b$  is the mass-spring system given by

$$2x'' + bx' + 6x = 0$$

underdamped? Sketch one such solution curve satisfying  $x(0) = x'(0) = 1$ .

2. Use the table to find the Laplace transform of the following.

(a) 

1
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 $f(t) = 4e^{-2t} + e^{2t} \sin 3t$

(b) 

1
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 $g(t) = \cos(3t) \sin(5t)$  [HINT: Product to Sum identity.]

3. 

2
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 Use the table of Laplace transforms to show

$$\mathcal{L} \left\{ \frac{1}{2}(\sin 3t - 3t \cos 3t) \right\} = \frac{27}{(s^2 + 9)^2}.$$

4. 4 Apply the Laplace transform to the initial value problem

$$y'' + 3y' + y = t \cos 2t, \quad y(0) = 1, y'(0) = -3$$

to express  $Y(s) = \mathcal{L}\{y(t)\}$  in the form  $Y(s) = \frac{P(s)}{Q(s)}$ ; i.e. the right-hand side should be a single combined fraction with the numerator multiplied out and the denominator factored into linear and/or irreducible quadratic terms.

**Do not find the inverse Laplace transform.**