Point values in boxes.

Math 274 Quiz 10 Section: 9.4 5 June 2018

1. $\boxed{1}$ The vectors

$$\mathbf{x}_1 = \begin{bmatrix} 1\\2\\3 \end{bmatrix}, \mathbf{x}_2 = \begin{bmatrix} 2\\-1\\0 \end{bmatrix}, \mathbf{x}_3 = \begin{bmatrix} 10\\0\\6 \end{bmatrix}$$

satisfy

 $2\mathbf{x}_1 + 4\mathbf{x}_2 - \mathbf{x}_3 = \mathbf{0}.$

The vectors $\mathbf{x}_1, \mathbf{x}_2, \mathbf{x}_3$ are linearly **independent** dependent on $(-\infty, \infty)$. (Circle one.)

2. 1 The vectors

$$\mathbf{x}_4 = \begin{bmatrix} 2e^t \\ 2 \end{bmatrix}, \mathbf{x}_5 = \begin{bmatrix} te^t \\ t \end{bmatrix}$$

satisfy

$$t\mathbf{x}_4 - 2\mathbf{x}_5 = \mathbf{0}$$
 for all t .

The vectors $\mathbf{x}_4, \mathbf{x}_5$ are linearly **independent/dependent** on $(-\infty, \infty)$. (Circle one.)

 $3. \ Let$

$$\mathbf{A} = \begin{bmatrix} 1 & -5 \\ 1 & -1 \end{bmatrix}, \mathbf{x}_1 = \begin{bmatrix} \cos 2t - 2\sin 2t \\ \cos 2t \end{bmatrix}, \mathbf{x}_2 = \begin{bmatrix} \sin 2t + 2\cos 2t \\ \sin 2t \end{bmatrix}$$
equation

and consider the equation

$$\mathbf{x}' = \mathbf{A}\mathbf{x}.\tag{1}$$

(a) 3 The vector function \mathbf{x}_1 is a solution to (1), verify \mathbf{x}_2 is also a solution to (1).

(b) 2 Verify $\{\mathbf{x}_1, \mathbf{x}_2\}$ is a fundamental solution set for (1).

(c) 1 Find a fundamental matrix for (1) and evaluate it at t = 0, i.e., find $\mathbf{X}(0)$.

(d) 2 Find the solution to the initial value problem

$$\mathbf{x}' = \mathbf{A}\mathbf{x}, \qquad \mathbf{x}(0) = \begin{bmatrix} 3\\1 \end{bmatrix}$$

You may find it useful to know that if $\mathbf{X} = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ is invertible then $\mathbf{X}^{-1} = \frac{1}{|\mathbf{X}|} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$.