Name: $\qquad$
Sections: 2.6,3.2, $\mathbb{C}$
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1. 5 Use an appropriate substitution to find a general solution to

$$
\frac{d y}{d x}=\frac{2 y^{2}-x^{2}}{x y} .
$$

2. A 100 L tank is initially filled with a sugar water solution with concentration $20 \mathrm{~g} / \mathrm{L}$. A solution of concentration $10 \mathrm{~g} / \mathrm{L}$ flows into the tank at $5 \mathrm{~L} / \mathrm{min}$. The tank is well mixed and the resulting mixture flows out at $5 \mathrm{~L} / \mathrm{min}$.
(a) 1 Sketch a graph of the amount of sugar in the tank (in g ) as a function of time.
(b) 3 Write an initial value problem, i.e. a differential equation with initial data, to model the amount of sugar in the tank. Do not solve.
(c) 1 If the mixture flows out at $7 \mathrm{~L} / \mathrm{min}$ instead of $5 \mathrm{~L} / \mathrm{min}$, write an initial value problem to model the amount of sugar in the tank. Do not solve.
