30 May 2018

1. 3 A graph of $y=f(t)$ is given below.


Find the Laplace transform of $f(t)$.
2. Assume $g(t)$ is piecewise continuous and of exponential order and consider the initial value problem

$$
y^{\prime \prime}+y^{\prime}=g(t), \quad y(0)=0, y^{\prime}(0)=0 .
$$

(a) 3 Find the solution. Express your solution in terms of a convolution.
(b) 1 Express the solution in terms of the appropriate convolution integral. Do not evaluate the integral.
(c) 3 If $g(t)=e^{-2 t}$, find the solution, i.e., evaluate the convolution.

