

## Stat 217, Practice Exam 2 Solutions

### Multiple Choice Problems

1. E (because the marbles are sampled with replacement)
2. A
3. There is no correct answer ... it should be  $N(100, 8.9443)$
4. A
5. B
6. D (the number of successes is the same as the number of 1s)
7. A

### Choose the correct Statistical Test

**C** chi-square

**B** test of two proportions

### Show Your Work Problems

8. (a) Let  $p_1$  be the proportion of dogs exposed to the herbicide that get lymphoma, and let  $p_2$  be the proportion of dogs not exposed to the herbicide that get lymphoma. The hypotheses are:

$$H_0 : p_1 = p_2$$

$$H_a : p_1 > p_2$$

- (b) The estimated proportions are:  $\hat{p}_1 = 473/827$ ,  $\hat{p}_2 = 19/130$ , the pooled estimate of  $p$  is  $\hat{p} = (473 + 19)/(827 + 130)$ . When you plug these into the formula for the two-sample test statistic you get:  $z = 9.0296$
  - (c)  $z \sim N(0, 1)$
  - (d) The p-value is  $P[z > 9.02] = 0.00$
  - (e) Since the p-value is less than .05 we REJECT  $H_0$
  - (f) The evidence suggests that dogs exposed to the herbicide are more likely to develop lymphoma.
9. Use the formula for sample size  $n = \left(\frac{z^*}{m}\right)^2 p(1-p)$  where  $z^* = 1.96$ ,  $m = .05$ , and  $p = .5$  (use  $p = .5$  to make sure the margin of error will be no greater than .05) and you get  $n = 385$ .
  10. (a)  $217/310 \pm \sqrt{\frac{(217/310)(1-217/310)}{310}} = (.64, .75)$ 
    - (b) We are 95% confident that the true proportion of college students who carry a credit card balance from month to month is between 64% and 75%. Thus, we are confident that the a majority of college students carry a credit card balance from month to month.
  11. (a) Conditional on the free-of-pain patients, we have 23/100 on Drug 1, 30/100 on Drug 2, 22/100 on Drug 3, and 25/100 on Drug 4.
    - (b) i.  $H_0$  : There is NO association between Pain and Drug Taken  
 $H_a$  : There is an association between Pain and Drug Taken
    - ii.  $(52)(95)/195 = 25.333$
    - iii.  $\frac{(25-23.08)^2}{23.08} = .1597$
    - iv.  $\chi^2$  with 3 degrees of freedom
    - v. Since the p-value of .184 is less than .05 we FAIL TO REJECT  $H_0$
    - vi. The evidence fails to suggest that there is an association between Pain and Drug Taken.
    - vii. D